

Based on ppt slides for CMSC 421 by B.J. Dorr

Artificial Intelligence I: knowledge representation

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Outline

- Ontological engineering
- Categories and objects
- Actions, situations and events
- Mental events and mental objects
- The internet shopping world
- Reasoning systems for categories
- Reasoning with default information
- Truth maintenance systems

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2

Ontological engineering

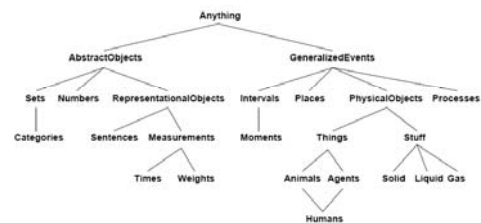
- How to create more general and flexible representations.
 - Concepts like actions, time, physical object and beliefs
 - Operates on a bigger scale than K.E.
- Define general framework of concepts
 - Upper ontology
- Limitations of logic representation
 - Red, green and yellow tomatoes: exceptions and uncertainty

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The upper ontology of the world



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Difference with special-purpose ontologies

- A general-purpose ontology should be applicable in more or less any special-purpose domain.
 - Add domain-specific axioms
- In any sufficiently demanding domain different areas of knowledge need to be unified.
 - Reasoning and problem solving could involve several areas simultaneously
- What do we need to express?
Categories, Measures, Composite objects, Time, Space, Change, Events, Processes, Physical Objects, Substances, Mental Objects, Beliefs

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Categories and objects

- KR requires the organisation of objects into categories
 - Interaction at the level of the object
 - Reasoning at the level of categories
- Categories play a role in predictions about objects
 - Based on perceived properties
- Categories can be represented in two ways by FOL
 - Predicates: apple(x)
 - Reification of categories into objects: apples
- Category = set of its members

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Category organization

- Relation = *inheritance*:
 - All instance of food are edible, fruit is a subclass of food and apples is a subclass of fruit then an apple is edible.
- Defines a taxonomy



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FOL and categories

- An object is a member of a category
 - $\text{MemberOf}(\text{BB}_{1,2}, \text{Basketballs})$
- A category is a subclass of another category
 - $\text{SubsetOf}(\text{Basketballs}, \text{Balls})$
- All members of a category have some properties
 - $\forall x (\text{MemberOf}(x, \text{Basketballs}) \Rightarrow \text{Round}(x))$
- All members of a category can be recognized by some properties
 - $\forall x (\text{Orange}(x) \wedge \text{Round}(x) \wedge \text{Diameter}(x) = 9.5 \text{in} \wedge \text{MemberOf}(x, \text{Balls}) \Rightarrow \text{MemberOf}(x, \text{Basketballs}))$
- A category as a whole has some properties
 - $\text{MemberOf}(\text{Dogs}, \text{DomesticatedSpecies})$

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Relations between categories

- Two or more categories are *disjoint* if they have no members in common:
 - $\text{Disjoint}(s) \Leftrightarrow \forall c_1, c_2. c_1 \in s \wedge c_2 \in s \wedge c_1 \neq c_2 \Rightarrow \text{Intersection}(c_1, c_2) = \{\}$
 - Example: $\text{Disjoint}(\{\text{animals}, \text{vegetables}\})$
- A set of categories s constitutes an *exhaustive decomposition* of a category c if all members of the set c are covered by categories in s :
 - $\text{E.D.}(s, c) \Leftrightarrow (\forall l \in c \Rightarrow \exists c_2. c_2 \in s \wedge l \in c_2)$
 - Example: $\text{ExhaustiveDecomposition}(\{\text{Americans}, \text{Canadian}, \text{Mexicans}, \text{NorthAmericans}\})$

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Relations between categories

- A *partition* is a disjoint exhaustive decomposition:
 - $\text{Partition}(s, c) \Leftrightarrow \text{Disjoint}(s) \wedge \text{E.D.}(s, c)$
 - Example: $\text{Partition}(\{\text{Males}, \text{Females}\}, \text{Persons})$.
- Is $(\{\text{Americans}, \text{Canadian}, \text{Mexicans}\}, \text{NorthAmericans})$ a partition?
- Categories can be defined by providing necessary and sufficient conditions for membership
 - $\forall x \text{ Bachelor}(x) \Leftrightarrow \text{Male}(x) \wedge \text{Adult}(x) \wedge \text{Unmarried}(x)$

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Natural kinds

- Many categories have no clear-cut definitions (chair, bush, book).
- Tomatoes: sometimes green, red, yellow, black. Mostly round.
- One solution: category *Typical(Tomatoes)*.
 - $\forall x, x \in \text{Typical}(\text{Tomatoes}) \Rightarrow \text{Red}(x) \wedge \text{Spherical}(x)$.
 - We can write down useful facts about categories without providing exact definitions.
- What about “bachelor”? Quine challenged the utility of the notion of *strict definition*. We might question a statement such as “the Pope is a bachelor”.

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Physical composition

- One object may be part of another:
 - $\text{PartOf}(\text{Bucharest}, \text{Romania})$
 - $\text{PartOf}(\text{Romania}, \text{EasternEurope})$
 - $\text{PartOf}(\text{EasternEurope}, \text{Europe})$
- The *PartOf* predicate is transitive (and irreflexive), so we can infer that $\text{PartOf}(\text{Bucharest}, \text{Europe})$
- More generally:
 - $\forall x \text{ PartOf}(x, x)$
 - $\forall x, y, z \text{ PartOf}(x, y) \wedge \text{PartOf}(y, z) \Rightarrow \text{PartOf}(x, z)$
- Often characterized by structural relations among parts.
 - E.g. $\text{Biped}(a) \Rightarrow$

$$\begin{aligned}
 & (\exists l_1, l_2, b) (\text{Leg}(l_1) \wedge \text{Leg}(l_2) \wedge \text{Body}(b) \wedge \\
 & \text{PartOf}(l_1, a) \wedge \text{PartOf}(l_2, a) \wedge \text{PartOf}(b, a) \wedge \\
 & \text{Attached}(l_1, b) \wedge \text{Attached}(l_2, b) \wedge \\
 & l_1 \neq l_2 \wedge (\forall l_3) (\text{Leg}(l_3) \Rightarrow (l_3 = l_1 \vee l_3 = l_2)))
 \end{aligned}$$

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12

Measurements

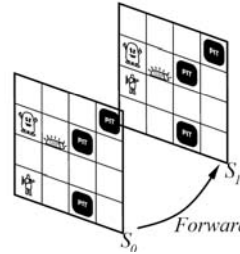
- Objects have height, mass, cost, ...
Values that we assign to these are **measures**
- Combine Unit functions with a number: $\text{Length}(L_1) = \text{Inches}(1.5) = \text{Centimeters}(3.81)$.
- Conversion between units:
 $\forall i \text{Centimeters}(2.54 \cdot i) = \text{Inches}(i)$.
- Some measures have no scale: Beauty, Difficulty, etc.
 - Most important aspect of measures: is that they are orderable.
 - Don't care about the actual numbers. (An apple can have deliciousness .9 or .1.)

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Actions, events and situations



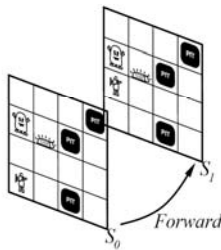
- Reasoning about outcome of actions is central to KB-agent.
- How can we keep track of location in FOL?
 - Remember the multiple copies in PL.
- Representing time by situations (states resulting from the execution of actions).
 - Situation calculus

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Actions, events and situations



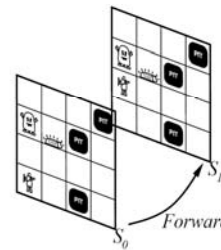
- Situation calculus:
 - Actions are logical terms
 - Situations are logical terms consisting of
 - The initial situation I
 - All situations resulting from the action on I ($= \text{Result}(a,s)$)
 - Fluent are functions and predicates that vary from one situation to the next.
 - E.g. $\neg \text{Holding}(G, S_0)$
 - Eternal predicates are also allowed
 - E.g. $\text{Gold}(G)$

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Actions, events and situations



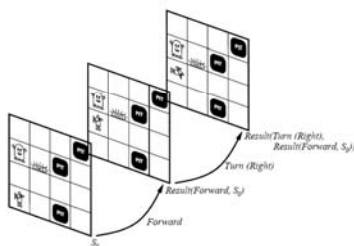
- Results of action sequences are determined by the individual actions.
- **Projection task:** an SC agent should be able to deduce the outcome of a sequence of actions.
- **Planning task:** find a sequence that achieves a desirable effect

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Actions, events and situations



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Describing change

- Simple Situation calculus requires two axioms to describe change:
 - Possibility axiom: when is it possible to do the action
 $At(\text{Agent}, x, s) \wedge \text{Adjacent}(x, y) \Rightarrow \text{Poss}(\text{Go}(x, y), s)$
 - Effect axiom: describe changes due to action
 $\text{Poss}(\text{Go}(x, y), s) \Rightarrow At(\text{Agent}, y, \text{Result}(\text{Go}(x, y), s))$
- What stays the same?
 - Frame problem: how to represent all things that stay the same?
 - Frame axiom: describe non-changes due to actions
 $At(o, x, s) \wedge (o \neq \text{Agent}) \wedge \neg \text{Holding}(o, s) \Rightarrow At(o, x, \text{Result}(\text{Go}(y, z), s))$

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Representational frame problem

- If there are F fluents and A actions then we need AF frame axioms to describe other objects are stationary unless they are held.
 - We write down the effect of each actions
- Solution; describe how each fluent changes over time
 - Successor-state axiom:
$$Poss(a,s) \Rightarrow (At(Agent,y,Result(a,s)) \Leftrightarrow (a = Go(x,y)) \vee (At(Agent,y,s) \wedge a \neq Go(y,z)))$$
 - Note that next state is completely specified by current state.
 - Each action effect is mentioned only once.

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Other problems

- How to deal with secondary (implicit) effects?
 - If the agent is carrying the gold and the agent moves then the gold moves too.
 - Ramification problem
- How to decide EFFICIENTLY whether fluents hold in the future?
 - Inferential frame problem.
- Extensions:
 - Event calculus (when actions have a duration)
 - Process categories

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Mental events and objects

- So far, KB agents can have beliefs and deduce new beliefs
- What about knowledge about beliefs? What about knowledge about the inference process?
 - Requires a model of the mental objects in someone's head and the processes that manipulate these objects.
- Relationships between agents and mental objects: believes, knows, wants, ...
 - Believes(Lois,Flies(Superman)) with Flies(Superman) being a function ... a candidate for a mental object (reification).
 - Agent can now reason about the beliefs of agents.

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The internet shopping world

- A Knowledge Engineering example
- An agent that helps a buyer to find product offers on the internet.
 - IN = product description (precise or -precise)
 - OUT = list of webpages that offer the product for sale.
- Environment = WWW
- Percepts = web pages (character strings)
 - Extracting useful information required.

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The internet shopping world

- Find relevant product offers
 - $$RelevantOffer(page,url,query) \Leftrightarrow Relevant(page,url,query) \wedge Offer(page)$$
 - Write axioms to define Offer(x)
 - Find relevant pages: Relevant(x,y,z) ?
 - Start from an initial set of stores.
 - What is a relevant category?
 - What are relevant connected pages?
 - Require rich category vocabulary.
 - Synonymy and ambiguity
 - How to retrieve pages: *GetPage(url)?*
 - Procedural attachment
- Compare offers (information extraction).

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Reasoning systems for categories

- How to organise and reason with categories?
 - Semantic networks
 - Visualize knowledge-base
 - Efficient algorithms for category membership inference
 - Description logics
 - Formal language for constructing and combining category definitions
 - Efficient algorithms to decide subset and superset relationships between categories.

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Semantic Networks

- Logic vs. semantic networks
- Many variations
 - All represent individual objects, categories of objects and relationships among objects.
- Allows for inheritance reasoning
 - Female persons inherit all properties from person.
 - Cfr. OO programming.
- Inference of inverse links
 - SisterOf vs. HasSister

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Semantic network example



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Semantic networks

- Drawbacks
 - Links can only assert binary relations
 - Can be resolved by reification of the proposition as an event
- Representation of default values
 - Enforced by the inheritance mechanism.

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Description logics

- Are designed to describe definitions and properties about categories
 - A formalization of semantic networks
- Principal inference task is
 - *Subsumption*: checking if one category is the subset of another by comparing their definitions
 - *Classification*: checking whether an object belongs to a category.
 - Consistency: whether the category membership criteria are logically satisfiable.

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Reasoning with Default Information

- “The following courses are offered: CS101, CS102, CS106, EE101”
 - Four (db)
 - Assume that this information is complete (not asserted ground atomic sentences are false)
 - = CLOSED WORLD ASSUMPTION
 - Assume that distinct names refer to distinct objects
 - = UNIQUE NAMES ASSUMPTION
 - Between one and infinity (logic)
 - Does not make these assumptions
 - Requires completion.

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Truth maintenance systems

- Many of the inferences have default status rather than being absolutely certain
 - Inferred facts can be wrong and need to be retracted = BELIEF REVISION.
 - Assume KB contains sentence P and we want to execute TELL(KB, ¬P)
 - To avoid contradiction: RETRACT(KB,P)
 - But what about sentences inferred from P?
- Truth maintenance systems are designed to handle these complications.

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30